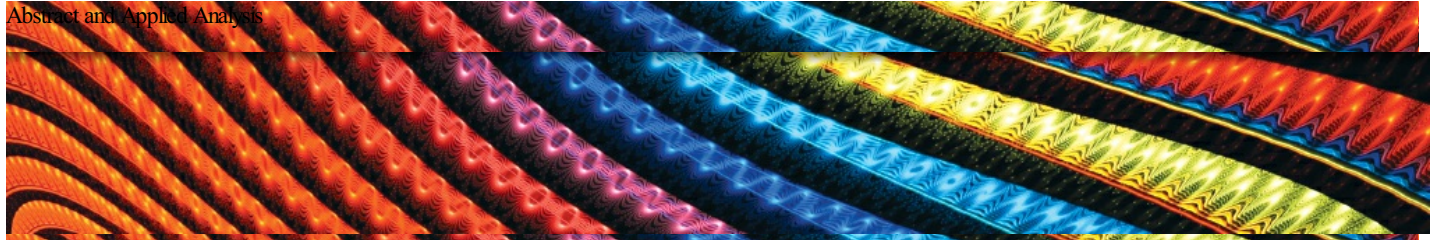


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Research Article

Null Field and Interior Field Methods for Laplace's Equation in Actually Punctured Disks

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